# The zeta function of $\mathfrak{g}_{147 B}$ counting ideals 

## 1 Presentation

$\mathfrak{g}_{147 B}$ has presentation

$$
\left\langle x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}, x_{7} \left\lvert\, \begin{array}{c}
{\left[x_{1}, x_{2}\right]=x_{4},\left[x_{1}, x_{3}\right]=x_{5},\left[x_{1}, x_{4}\right]=x_{7},} \\
{\left[x_{2}, x_{6}\right]=x_{7},\left[x_{3}, x_{5}\right]=x_{7}}
\end{array}\right.\right\rangle .
$$

$\mathfrak{g}_{147 B}$ has nilpotency class 3 .

## 2 The local zeta function

The local zeta function was first calculated by Luke Woodward. It is

$$
\begin{aligned}
\zeta_{\mathfrak{g}_{147 B}, p}^{\triangleleft}(s)= & \zeta_{p}(s) \zeta_{p}(s-1) \zeta_{p}(s-2) \zeta_{p}(s-3) \zeta_{p}(3 s-4) \zeta_{p}(3 s-5) \zeta_{p}(5 s-8) \\
& \times \zeta_{p}(7 s-6) \zeta_{p}(6 s-8)^{-1}
\end{aligned}
$$

$\zeta_{\mathfrak{g}_{147 B}}^{\triangleleft}(s)$ is uniform.

## 3 Functional equation

The local zeta function satisfies the functional equation

$$
\left.\zeta_{\mathfrak{g}_{147 B}, p}^{\triangleleft}(s)\right|_{p \rightarrow p^{-1}}=-p^{21-16 s} \zeta_{\mathfrak{g}_{147 B}, p}^{\triangleleft}(s) .
$$

## 4 Abscissa of convergence and order of pole

The abscissa of convergence of $\zeta_{\mathfrak{g}_{147 B}}^{\triangleleft}(s)$ is 4 , with a simple pole at $s=4$.

## 5 Ghost zeta function

This zeta function is its own ghost.

## 6 Natural boundary

$\zeta_{\mathfrak{g}_{147 B}}^{\triangleleft}(s)$ has meromorphic continuation to the whole of $\mathbb{C}$.

## 7 Notes

This ideal zeta function is identical to that of $\mathfrak{g}_{147 A}$, though the Lie rings themselves are non-isomorphic.

